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Low-Energy Electron Diffraction

Experiment, Theory and Surface Structure Determination

With 213 Figures

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