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Differential Equations and Their Applications
An Introduction to Applied Mathematics

Fourth Edition

With 68 Illustrations

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First-order differential equations 1

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